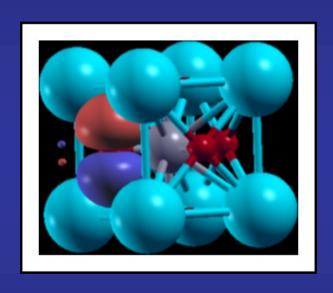
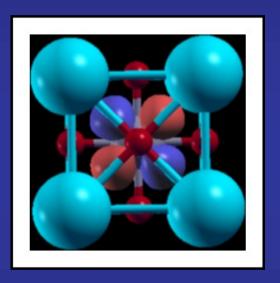
# How to run WANNIER90 directly from SIESTA





Javier Junquera



### **Important bibliography:**

#### For a review on Maximally Localized Wannier functions:

REVIEWS OF MODERN PHYSICS, VOLUME 84, OCTOBER-DECEMBER 2012

#### Maximally localized Wannier functions: Theory and applications

#### Nicola Marzari

Theory and Simulation of Materials (THEOS), École Polytechnique Fédérale de Lausanne, Station 12, 1015 Lausanne, Switzerland

#### Arash A. Mostofi

Departments of Materials and Physics, and the Thomas Young Centre for Theory and Simulation of Materials, Imperial College London, London SW7 2AZ, United Kingdom

#### Jonathan R. Yates

Department of Materials, University of Oxford, Parks Road, Oxford OX1 3PH, United Kingdom

#### Ivo Souza

Centro de Física de Materiales (CSIC) and DIPC, Universidad del País Vasco, 20018 San Sebastián, Spain and Ikerbasque Foundation, 48011 Bilbao, Spain

#### **David Vanderbilt**

Department of Physics and Astronomy, Rutgers University, Piscataway, New Jersey 08854-8019, USA

### **Important bibliography:**

The user guide of the WANNIER90 code

wannier90: User Guide

Version 3.0

27th February 2019

Freely available from: http://www.wannier.org

#### WANNIER90 code directly called from SIESTA

WANNIER90 code (version 3.0.0) has been compiled in library mode and called directly from SIESTA

That means that we can run all the functionalities of WANNIER90 directly from SIESTA

#### **Advantages**

- No need to prepare two different input files
- No need to run WANNIER90 in pre-processing mode
- We can use the basis set of SIESTA (numerical atomic orbitals) as the initial guess for the projections
- Wannierization of different manifolds can be done in the same run of SIESTA
- The unitary matrices connecting the Bloch and Wannier representations are available in SIESTA.

New functionalities can follow (initial guesses for order-N simulations)

Interface with other codes will be much easier:

**SCALE-UP** (second-principles)

**DMFTwDFT (DMFT code by Aldo Romero's group)** 

## **WANNIER90** code directly called from SIESTA

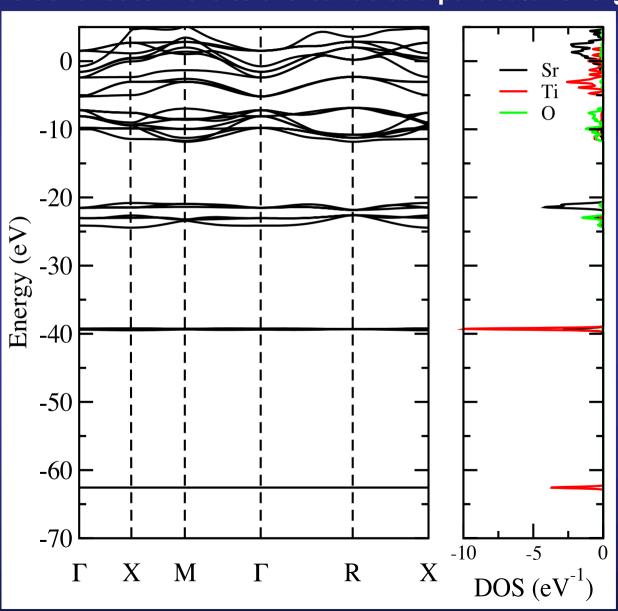
Practical examples:

Bulk SrTiO<sub>3</sub> in the cubic phase

Graphene

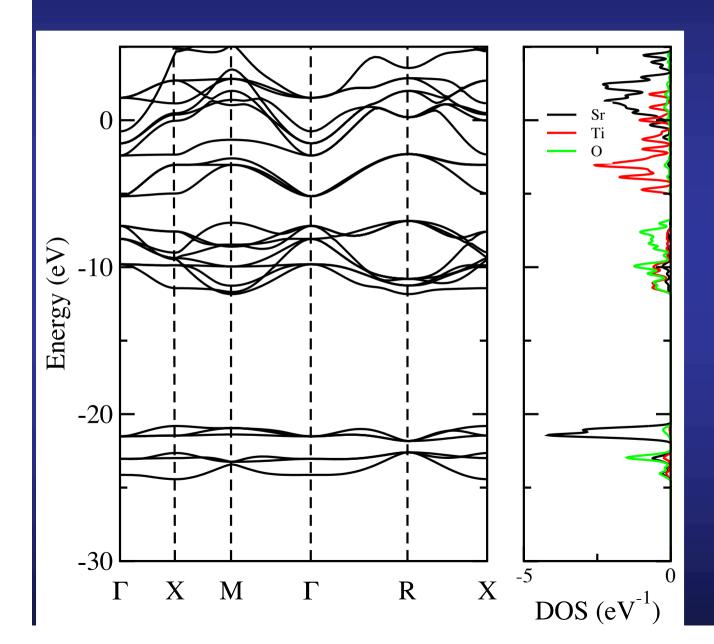
## After running SIESTA and compute the PDOS, we can analyze the character of the different bands

Which atoms contribute more to the bands at a particular energy window



#### We can analyze the character of the different bands

Which atoms contribute more to the bands at a particular energy window Zoom around the top of the valence bands and bottom of conduction bands



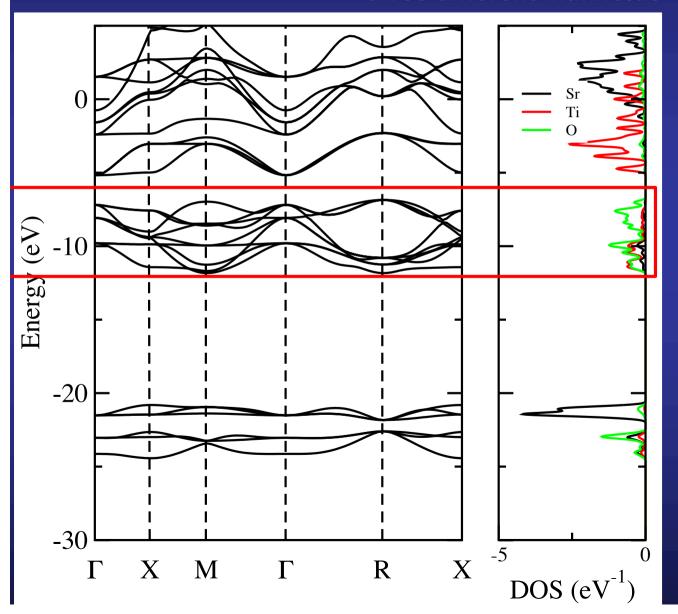
Bottom of conduction bands mostly Ti t<sub>2q</sub> character

Top of valence bands: mostly O 2p character

We can project on particular atomic orbitals within an atom to further define the character.

## Choose the Bloch states that will be used to compute the Wannier functions

In this particular example, we are interested in the wannierization of three different manifolds



Manifold number 1:

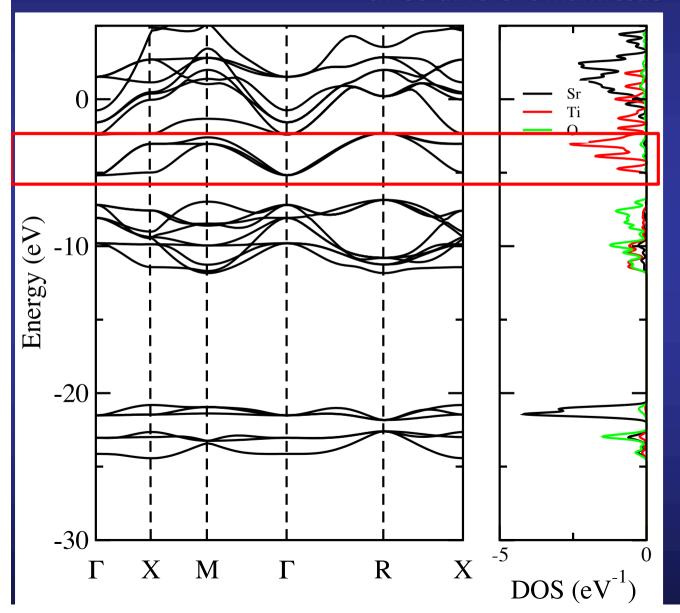
Top of valence bands: mostly O 2*p* character

That means: - 3 O p bands  $(p_x, p_y, p_z)$ × 3 O atoms

9 bands to wannierize

## Choose the Bloch states that will be used to compute the Wannier functions

In this particular example, we are interested in the wannierization of three different manifolds



Manifold number 2:

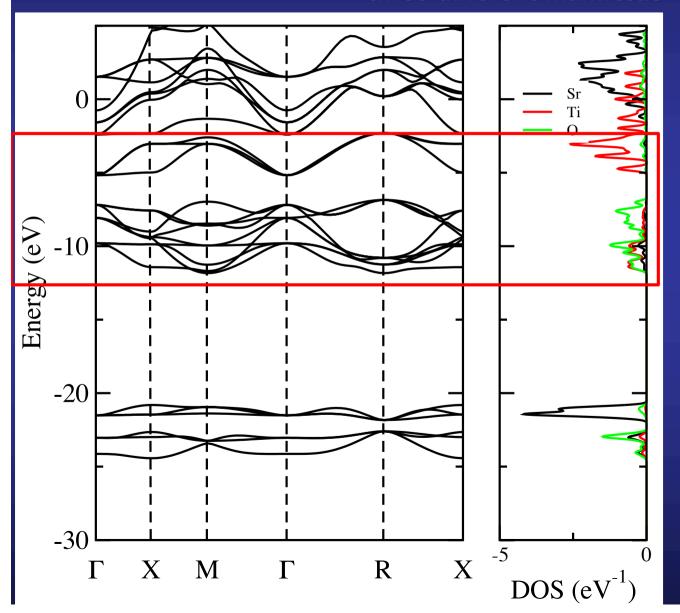
Bottom of conduction bands: mostly Ti t<sub>2g</sub> character

That means: -3 Ti  $t_{2g}$  bands  $(d_{xy}, d_{yz}, d_{xz})$ 

3 bands to wannierize

## Choose the Bloch states that will be used to compute the Wannier functions

In this particular example, we are interested in the wannierization of three different manifolds



**Manifold number 3:** 

Bottom of conduction bands: mostly Ti t<sub>20</sub> character

Top of valence bands: mostly O 2*p* character

**That means:** 

- 3 O p bands  $(p_x, p_y, p_z)$ × 3 O atoms
- 3 Ti  $t_{2g}$  bands  $(\overline{d_{xy}, d_{yz}, d_{yz}}, \overline{d_{xz}})$

12 bands to wannierize

Number of manifolds to wannierize

%block WannierManifolds
first
second
third
%endblock

As many lines in the block as manifolds will be wannierized

A nickname is given to each manifold

#### Information for every manifold

As many WannierManifolds blocks as manifolds considered for wannierization

## The nickname of every manifold is appended here to the keyword WannierManifold

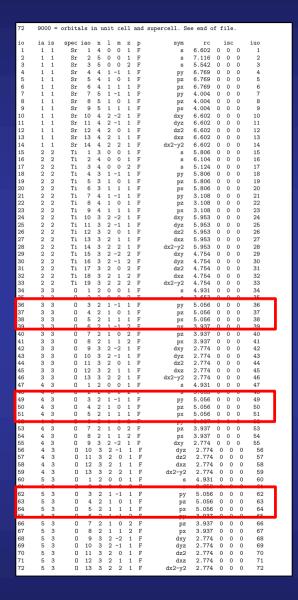
```
%block WannierManifold.first
  # Indices of the initial and final band of the manifold
 bands 12 20
  # Indices of the orbitals that will be used as localized trial orbitals
      (any number of lines allowed)
 trial-orbitals [36 37 38]
 trial-orbitals [49 50 51]
 trial-orbitals [62 63 64]
  # Number of iterations for the minimization of \Omega
  spreading.nitt 0
 wannier_plot 3
  fermi_surface_plot true
 write hr true
 write_tb true
%endblock
```

```
%block WannierManifold.first
  # Indices of the initial and final band of the manifold
  bands 12 20
  # Indices of the orbitals that will be used as localized trial orbitals
       (any number of lines allowed)
  trial-orbitals [36 37 38]
  trial-orbitals [49 50 51]
  trial-orbitals [62 63 64]
  # Number of iterations for the minimization of \Omega
  spreading.nitt 0
  wannier_plot 3
  fermi_surface_plot true
  write hr true
  write tb true
%endblock
              ! For every k-point, the bands in Siesta are ordered from lowest to highest
              ! energy
              ! The character of the bands are known after computation of the PDOS.
              ! In order, for the case of SrTiO3:
              ! Bands to be excluded
              ! Band 1 (lowest band): Ti-3s character
             ! Bands 2, 3, and 4: Ti-3p character (px, py, and pz)
! Band 5: Sr-4s character
              ! Bands 6, 7, and 8: 0-2s character (1 band * 3 0 atoms in the unit cell)
              ! Bands 9, 10, and 11: Sr-4p character (px, py, and pz)
              ! Bands to be wannierized
             ! Bands 12-20: 0-2p character (3 bands * 3 0 atoms in the unit cell
             ! Bands 21, 22, and 23: Ti-t2g characer (dxy, dyz, dxz)
```

```
%block WannierManifold.first
    # Indices of the initial and final band of the manifold
    bands 12 20

# Indices of the orbitals that will be used as localized trial orbitals
    # (any number of lines allowed)
    trial-orbitals [36 37 38]
    trial-orbitals [49 50 51]
    trial-orbitals [62 63 64]

# Number of iterations for the minimization of \Omega
    spreading.nitt 0
    wannier_plot 3
    fermi_surface_plot true
    write_hr true
    write_tb true
%endblock
```



A good initial guess to project the bands of the top of the valence band are the O-2p orbitals

Take a look to the SystemLabel.ORB\_INDX file

p-orbitals of the first O atom

p-orbitals of the second O atom

*p*-orbitals of the third O atom

```
%block WannierManifold.first
  # Indices of the initial and final band of the manifold
 bands 12 20
  # Indices of the orbitals that will be used as localized trial orbitals
      (any number of lines allowed)
 trial-orbitals [36 37 38]
 trial-orbitals [49 50 51]
 trial-orbitals [62 63 64]
 # Number of iterations for the minimization of \Omega
 spreading.nitt 0
  wannier_plot 3
  fermi_surface_plot true
 write hr true
 write tb true
%endblock
```

Number of iterations for the minimization of the localization functional

If zero, then the procedure is the same as a Löwdin orthonormalization

The resulting Wannier functions will keep the symmetry of the projection function, but it will not be maximally localized

```
%block WannierManifold.first
  # Indices of the initial and final band of the manifold
  bands 12 20
  # Indices of the orbitals that will be used as localized trial orbitals
  # (any number of lines allowed)
  trial-orbitals [36 37 38]
  trial-orbitals [49 50 51]
  trial-orbitals [62 63 64]
  # Number of iterations for the minimization of \Omega
  spreading.nitt 0
  wannier_plot 3
  fermi_surface_plot true
  write_hr true
  write_tb true
%endblock
```

#### **Instruction to plot the Wannier functions**

The integer refers to the size of the supercell for plotting the Wannier functions

```
%block WannierManifold.first
  # Indices of the initial and final band of the manifold
 bands 12 20
  # Indices of the orbitals that will be used as localized trial orbitals
      (any number of lines allowed)
 trial-orbitals [36 37 38]
 trial-orbitals [49 50 51]
 trial-orbitals [62 63 64]
 # Number of iterations for the minimization of \Omega
  spreading.nitt 0
 wannier plot 3
 fermi_surface_plot true
 write hr true
 write tb true
%endblock
```

Flag to determine whether the Fermi Surface is computed or not

```
%block WannierManifold.first
    # Indices of the initial and final band of the manifold
    bands 12 20
    # Indices of the orbitals that will be used as localized trial orbitals
    # (any number of lines allowed)
    trial-orbitals [36 37 38]
    trial-orbitals [49 50 51]
    trial-orbitals [62 63 64]
    # Number of iterations for the minimization of \Omega
    spreading.nitt 0
    wannier_plot 3
    fermi_surface_plot true
    write_hr true
    write_tb true
%endblock
```

Flag to determine whether the Hamiltonian in real space in a basis of Wannier functions is written

SystemLabel.manifold.X\_hr.dat

X is the nickname of the manifold

```
%block WannierManifold.first
    # Indices of the initial and final band of the manifold
    bands 12 20
    # Indices of the orbitals that will be used as localized trial orbitals
    # (any number of lines allowed)
    trial-orbitals [36 37 38]
    trial-orbitals [49 50 51]
    trial-orbitals [62 63 64]
    # Number of iterations for the minimization of \Omega
    spreading.nitt 0
    wannier_plot 3
    fermi_surface_plot true
    write hr true
    write_tb true
%endblock
```

Flag to determine whether the lattice vectors, Hamiltonian in real space and position operator in a basis of Wannier functions are written

SystemLabel.manifold.X\_tb.dat

X is the nickname of the manifold

Wannier.k [4 4 4]

Number of k-points used in the Wannierization

#### **Successful output of SIESTA**

```
switch_local_projection: Populating the relevant matrices for
switch_local_projection: calling WANNIER90 directly from SIESTA
switch_local_projection: band manifold = first
compute_pw_matrix: Computing the matrix elements of a plane wave
mmn: Overlap matrices between periodic part of wavefunctions
mmn: written in w90 in siesta.manifold.first.mmn file
amn: Overlap matrices between trial projection functions and wavefunctions
amn: written in w90_in_siesta.manifold.first.amn file
eig: Eigenvalues of the Hamiltonian
eig: written in w90_in_siesta.manifold.first.eigW file
compute_matrices: All the information dumped in the corresponding files
compute_matrices: End of the interface between Siesta and Wannier90
... Calling wannier90 for this manifold
... See file w90_in_siesta.manifold.first.wout for information
```

### **Successful output of SIESTA**

** ++< CONV			
	RMS Gradient Spread (Ang^2)	Time  < CONV	
+		+< CONV	
Initial State			
WF centre and spread	1 (-0.000000, 1.937000, 1.937000	) 1.28449725	
WF centre and spread	2 (-0.000000, 1.937000, 1.937000		
WF centre and spread	3 ( 0.000000, 1.937000, 1.937000		
WF centre and spread	4 ( 1.937000, -0.000000, 1.937000	) 1.17470279	
WF centre and spread	5 ( 1.937000, 0.000000, 1.937000	) 1.28449725	
WF centre and spread	6 ( 1.937000, -0.000000, 1.937000	) 1.28449725	
WF centre and spread	7 ( 1.937000, 1.937000, 0.000000	) 1.28449726	
WF centre and spread	8 ( 1.937000, 1.937000, 0.000000	) 1.17470278	
WF centre and spread	9 ( 1.937000, 1.937000, 0.000000		
Sum of centres and spre	ads (11.622000, 11.622000, 11.622000	) 11.23109189	
0 0.112E+02			
O_D= 0.00000	00 O_OD= 0.1485757 O_TOT= 11.5	2310919 < SPRD	
Final State			
WF centre and spread	1 (-0.000000, 1.937000, 1.937000	) 1.28449725	
WF centre and spread	2 (-0.000000, 1.937000, 1.937000	) 1.28449725	
WF centre and spread	3 ( 0.000000, 1.937000, 1.937000		
WF centre and spread	4 ( 1.937000, -0.000000, 1.937000		
WF centre and spread	5 ( 1.937000, 0.000000, 1.937000		
WF centre and spread	6 ( 1.937000, -0.000000, 1.937000		
WF centre and spread	7 ( 1.937000, 1.937000, 0.000000		
WF centre and spread	8 ( 1.937000, 1.937000, 0.000000		
WF centre and spread	9 ( 1.937000, 1.937000, 0.000000		
Sum of centres and spre	ads (11.622000, 11.622000, 11.622000	) 11.23109189	
(0	Omega I = 11.082516189		
Spreads (Ang^2)	Omega I = 11.082516189 Omega D = 0.000000000		
	Omega D = 0.000000000 Omega OD = 0.148575697		
Final Spread (Ang^2)	Omega UD = 0.1485/569/ Omega Total = 11.231091885		
Spread (Ang 2)			
Time for wannierise	0.002 (sec)		

## The output is exactly the same as the WANNIER90 code

9 WF centered on the three O
The spread of the Wannier
functions (in Å) is three and six
fold degenerated

#### **How to plot the Wannier functions**

First of all, SIESTA has to write the periodic part of the Bloch functions in a 3D grid. The number of points in the grid along the three lattice vectors are given by

seedname.fdf file (input of SIESTA)

Wannier.Manifolds.Unk	.true.	
Siesta2Wannier90.UnkGri Siesta2Wannier90.UnkGri Siesta2Wannier90.UnkGri	d2	30 30 30

This produces many files with the name UNKXXXXX.Y where

- XXXXX is the number of the k-point, from 1 to the number of points included in seedname.win file
- Y refers to the spin component (1 or 2)

#### **How to plot the Wannier functions**

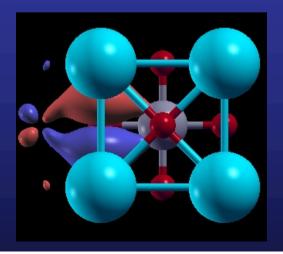
Wannier90 produces files with the name: SystemLabel.manifold.X\_0000Y.xsf that can be directly plotted with XCRYSDEN

Once XCrySDen starts, click on File → Open structure (Select your xsf file)

Tools → Data Grid

Click on OK
Then, select:
Degree of triCubic Spline: 3
Click on Render+/- isovalue
Select the desired isovalue (in this example 0.1)
Submit

SrTiO3.manifold.first\_00001.xsf



## **WANNIER90** code directly called from SIESTA

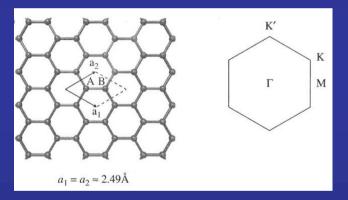
Practical examples:
Bulk SrTiO<sub>3</sub> in the cubic phase
Graphene

## Graphene, including bond centered Hydrogen ghost atoms

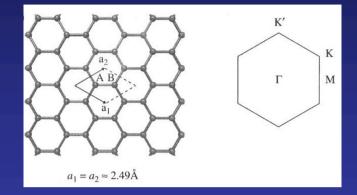
```
SystemName
                   graphene
                   Graphene layer
                   Ghost atoms included at the center of the bonds
                   MeshCutoff: 600 Ry
                   20 x 20 x 1 Monkhorst-Pack mesh
SystemLabel
                   graphene
NumberOfAtoms
                                 # Number of atoms in the unit cell
                                 # We include here:
                                 # - The two carbon atoms of the motif
                                 # - Three Hydrogen ghost atoms at the center
                                    of the bonds between first-neighbors
                                 # Only the atomic orbitals of the atoms
                                    will be included in the simulation,
                                 # while the atomic nuclei will not be
                                 # considered
NumberOfSpecies
                                 # Number of different atomic species in the
                                     simulation.
                                 # We include here:
                                 # - C (with an atomic number of 6)
                                 # - pseudo-Hydrogen atom
                                 # (with an atomic number of -1)
%block ChemicalSpeciesLabel
                                # Chemical species label as indicated above
     6 C
  2 -1 Ghost-H
%endblock ChemicalSpeciesLabel
```

#### **Graphene: atomic structure in SIESTA**

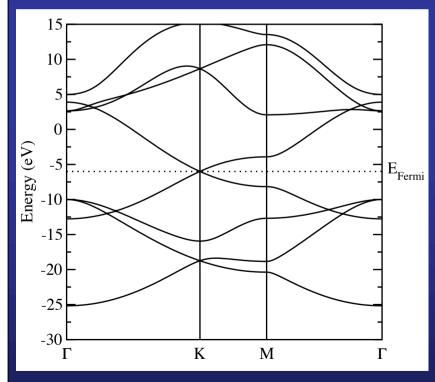
```
# Atomic structure: lattice vectors and atomic coordinates
LatticeConstant
                   1.46700 Ang # Nearest-neighbor distance, d
                              # The primitive translation vectors
                                 will be given by
                                 a_{1} = (3/2 d, - sqrt(3)/2 d, 0)
                                 a_{2} = (3/2 d, + sqrt(3)/2 d, 0)
                                 Here the z-component of the vectors
                                 is large enough to avoid interactions
                                 between periodic replicas of the slab
%block LatticeVectors
  1.500000000
                   -0.8660254038
                                      0.000000000
  1.500000000
                    0.8660254038
                                      0.000000000
  0.00000000
                    0.000000000
                                     20.0000000000
%endblock LatticeVectors
AtomicCoordinatesFormat Fractional
%block AtomicCoordinatesAndAtomicSpecies
  0.666666667 0.6666666667 0.0000000000 1
  0.500000000 0.500000000 0.000000000 2
  0.500000000 0.000000000 0.000000000 2
  0.000000000 0.500000000
                             0.0000000000 2
%endblock AtomicCoordinatesAndAtomicSpecies
%block kgrid_Monkhorst_Pack
          0.0
          0.0
        1 0.0
%endblock Kgrid_Monkhorst_Pack
```



#### Graphene: plotting the band-structure in SIESTA

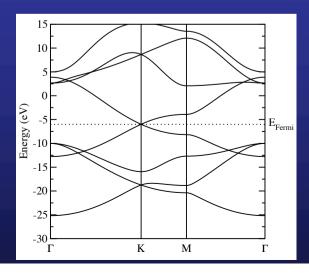


```
# Plotting the band structure
BandLinesScale
                   ReciprocalLatticeVectors
%block BandLines
    0.0
                                         # Begin at \Gamma
             0.0
                        0.0
                              \Gamma
                                         # 50 points from \Gamma to K
   0.33333 0.666667
                        0.0
                                         # 50 points from K to M
   0.5
             0.5
                        0.0
                                         # 50 points from M to \Gamma
   0.0
             0.0
                        0.0
                            \Gamma
%endblock BandLines
# Plotting the Projected Density Of States
%block ProjectedDensityOfStates
  -70.00 5.00 0.150 3000 eV
%endblock ProjectedDensityOfStates
%PDOS.kgrid_Monkhorst_Pack
   60 0 0 0.5
    0 60 0 0.5
    0 0 2 0.5
%end PDOS.kgrid_Monkhorst_Pack
```



#### WANNIER90 code directly available from SIESTA

```
%block WannierManifold first
 # Indices of the initial and final band of the manifold
             8
  bands 1
 # Indices of the orbitals that will be used as localized trial orbitals
      (any number of lines allowed)
 trial-orbitals [9 10 11 3 7]
 # Number of iterations for the minimization of \Omega
  spreading.nitt 0
 wannier_plot 3
 fermi_surface_plot true
 write_hr true
 write_tb true
 # Bottom and top of the outer energy window for band disentanglement (in eV)
                         5.0 eV
                -30.0
  window
 # Bottom and top of the inner energy window for band disentanglement (in eV)
 window.frozen -30.0
                        -7.5 \, eV
%endblock
```

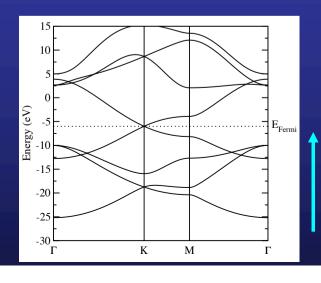


## We have eight bands in the outer energy window

We are interested in project over the wannierization over the three sp² orbitals and the  $\pi/\pi$  manifold (five Wannier functions in total)

#### WANNIER90 code directly available from SIESTA

```
%block WannierManifold first
 # Indices of the initial and final band of the manifold
  bands 1
 # Indices of the orbitals that will be used as localized trial orbitals
      (any number of lines allowed)
 trial-orbitals [9 10 11 3 7]
 # Number of iterations for the minimization of \Omega
  spreading.nitt 0
 wannier_plot 3
 fermi_surface_plot true
 write_hr true
 write_tb true
 # Bottom and top of the outer energy window for band disentanglement (in eV)
                         5.0 eV
                -30.0
 window
 # Bottom and top of the inner energy window for band disentanglement (in eV)
 window.frozen -30.0 -7.5 eV
%endblock
```



Frozen energy window

Some Bloch states are forced to be preserved identically in the projected manifold; those are referred to as belonging to a frozen "inner" window

We are interested in project over the wannierization over the three sp² orbitals and the  $\pi/\pi^*$ manifold (five Wannier functions in total)

### Output of a succesful run

```
-----*
 Iter Delta Spread RMS Gradient
                                      Spread (Ang^2)
Initial State
WF centre and spread
                      1 ( 2.200500, 0.000000, 0.000000)
                                                             0.71294917
                      2 ( 1.100250, -0.635230, 0.000000 )
WF centre and spread
                                                             0.71294809
WF centre and spread
                      3 ( 1.100250, 0.635230, 0.000000 )
                                                             0.71294809
WF centre and spread
                      4 ( 1.467000, -0.000000, 0.000000 )
                                                             0.81286407
WF centre and spread
                      5 ( 2.933999, -0.000000, 0.000000 )
                                                             0.81286543
Sum of centres and spreads ( 8.801998, -0.000000, 0.000000)
                                                             3.76457484
         0.376E+01
                      0.0000000000
                                        3.7645712185
                                                         0.04 <-- CONV
      O_D= 0.0016044 O_OD=
                                  0.7962785 O_TOT=
                                                     3.7645712 <-- SPRD
Final State
WF centre and spread
                      1 ( 2.200500, 0.000000, 0.000000)
                                                             0.71294917
                      2 ( 1.100250, -0.635230, 0.000000 )
WF centre and spread
                                                             0.71294809
WF centre and spread
                      3 ( 1.100250, 0.635230, 0.000000 )
                                                             0.71294809
WF centre and spread
                      4 ( 1.467000, -0.000000, 0.000000)
                                                             0.81286407
WF centre and spread
                      5 ( 2.933999, -0.000000, 0.000000 )
                                                             0.81286543
Sum of centres and spreads ( 8.801998, -0.000000, 0.000000)
                                                             3.76457484
                                      = 2.966688302
       Spreads (Ang^2)
                          Omega I
      ==========
                          Omega D
                                      = 0.001604421
                          Omega OD
                                    = 0.796278495
  Final Spread (Ang^2)
                          Omega Total =
                                           3.764571218
Time for wannierise
                           0.004 (sec)
```

Three sp<sub>2</sub> type-Wanniers The  $\pi/\pi^*$  manifold

### How to plot the Wannier functions

Wannier90 produces files with the name: SystemLabel.manifold.X\_0000Y.xsf that can be directly plotted with XCRYSDEN

Once XCrySDen starts, click on

File  $\rightarrow$  Open structure (Select your xsf file)
Modify  $\rightarrow$  Number of units drawn 2 (along x) 2 (along y) 1 (along z)
Tools  $\rightarrow$  Data Grid

Click on OK
Then, select:

Degree of triCubic Spline: 3

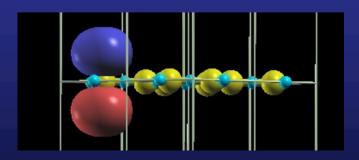
Click on Render+/- isovalue

Select the desired isovalue (in this example 0.1)

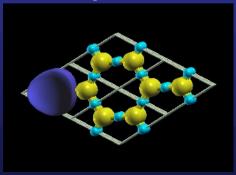
**Submit** 

graphene.manifold.first\_00004.xsf

**Lateral view** 



Top view



#### **Funding**

## SPANISH INITIATIVE FOR ELECTRONIC SIMULATIONS WITH THOUSANDS OF ATOMS: CÓDIGO ABIERTO CON GARANTÍA Y SOPORTE PROFESIONAL: SIESTA-PRO

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"Promover el desarrollo tecnológico, la innovación y una investigación de calidad"



