

# Converge calculations

Mesh, k-points and SCF convergence

Catalina Coll

3th October 2023



# Quality/accuracy/precision

<b>Monday 2nd October</b>	
12:30–12:45	Introductory remarks
12:45–13:30	General Siesta Theory (Prof. José Soler, UAM)
13:30–13:55	Pseudopotentials (Dr. Alberto García, ICMAB-CSIC)
13:55–14:10	Break
14:10–16:00	A first contact with SIESTA: inputs, execution and outputs (Dr. Federico Pedron, ICN2)
16:00–16:15	Break
16:15–17:15	Basis sets in SIESTA (Dr. Miguel Pruneda, CINN-CSIC)
17:15–17:30	Discussion and feedback
<b>Tuesday 3rd October</b>	
12:30–14:30	Basis set optimization (Dr. Federico Pedron, ICN2)
14:30–14:45	Break
14:45–16:15	K-points, mesh, and SCF convergence (Dr. Catalina Coll, ICN2)

System geometry

Pseudo potential

Real space grid

SCF convergence parameters

Basis Set

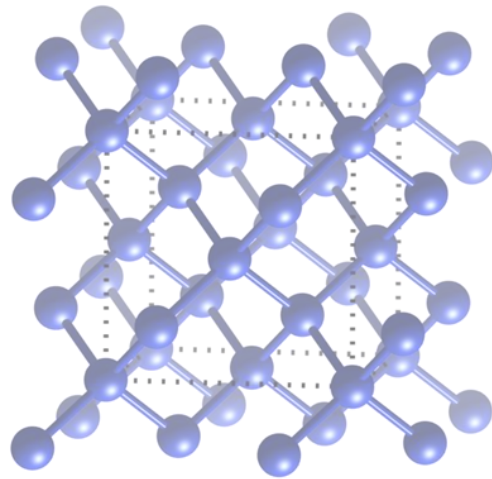
Reciprocal space grid

# Sampling

# Sampling

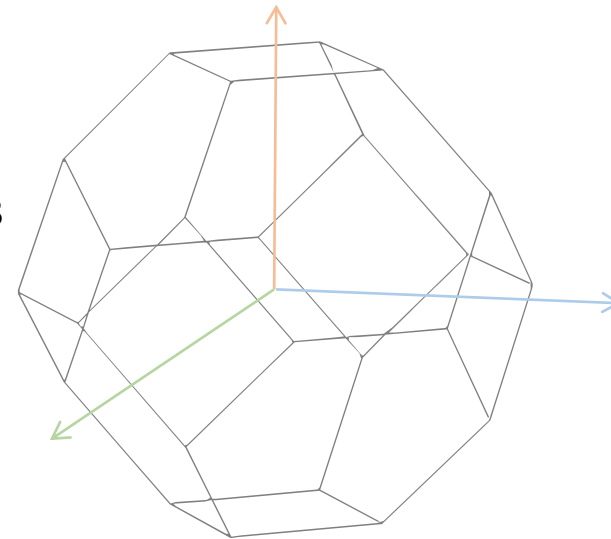
## Real space

- Potentials
- Densities
- Basis

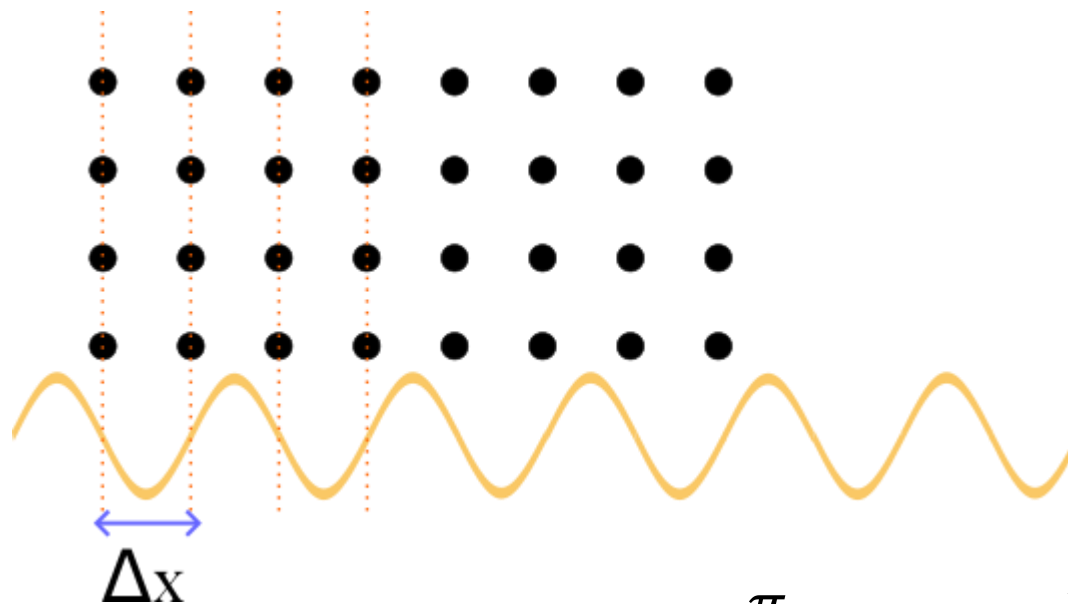
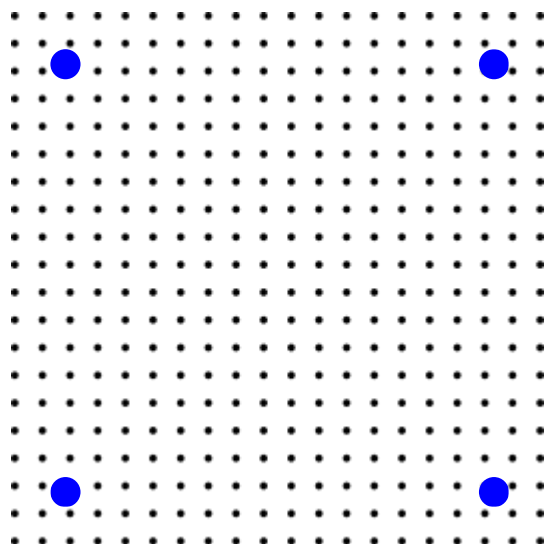


## Reciprocal space

- Density of states
- Bandstructure



# Real space grid



$$\Delta x \rightarrow k_c = \frac{\pi}{\Delta x} \rightarrow E_c = \frac{\hbar^2 k_c^2}{2m_e}$$

Fineness  $\leftrightarrow$  Maxim energy avoiding aliasing

$$\Delta x \leftrightarrow E_c \quad \text{MeshCutoff}$$

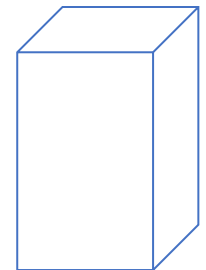
Energy units (Ry)

# Real space grid: MeshCutoff

- What is it set by the user?
  - Mesh.Cutoff 300 Ry (default)
- What is set by siesta?
  - MESH =  $18 \times 18 \times 30 = 9720$
  - Mesh cutoff (required, used) = 100.000 101.039 Ry
- How can one decide the good value?
  - Minimize the total energy.
  - Total force to zero.
  - Reasonable time (relatively small systems)

```
Mesh.Cutoff 100 Ry
```

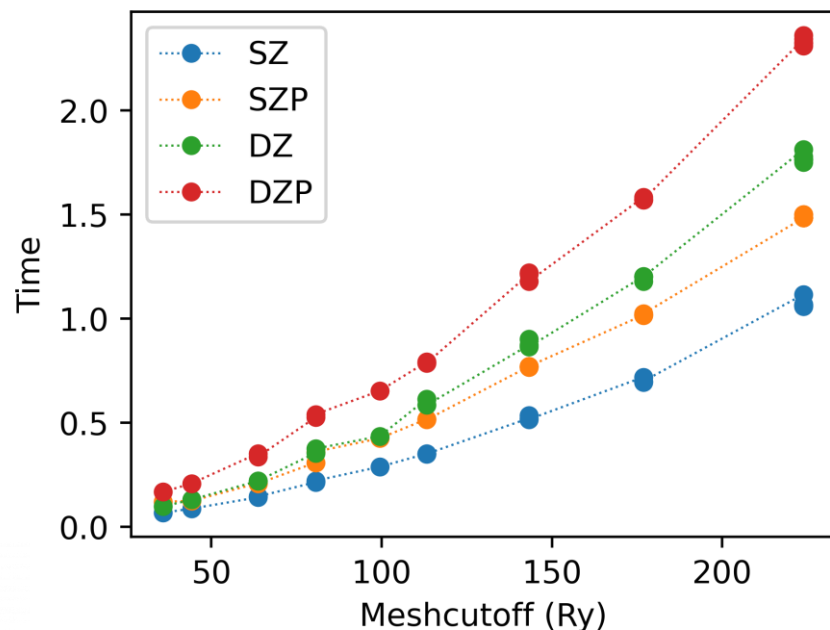
Input structure  $\longrightarrow$  Lattice vectors



# Real space grid: MeshCutoff

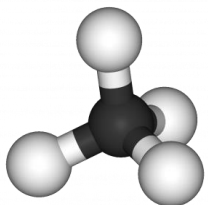
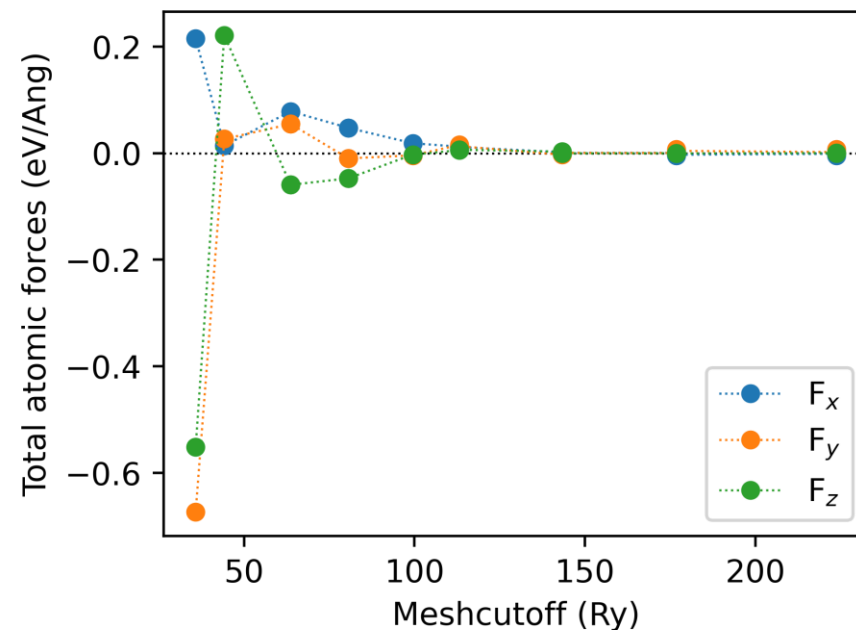
Time

TIMES file



Force

siesta: Atomic forces (eV/Ang):

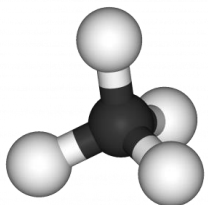
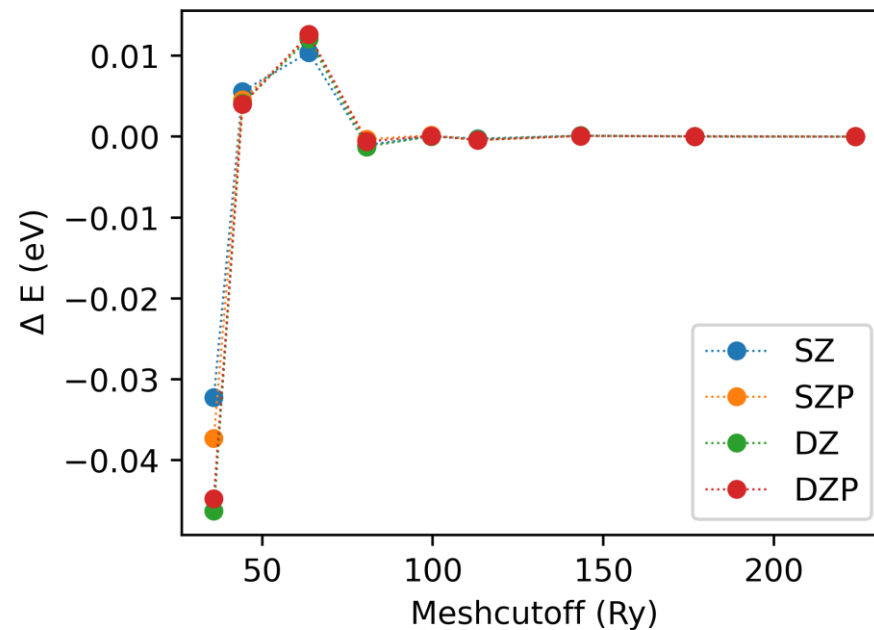
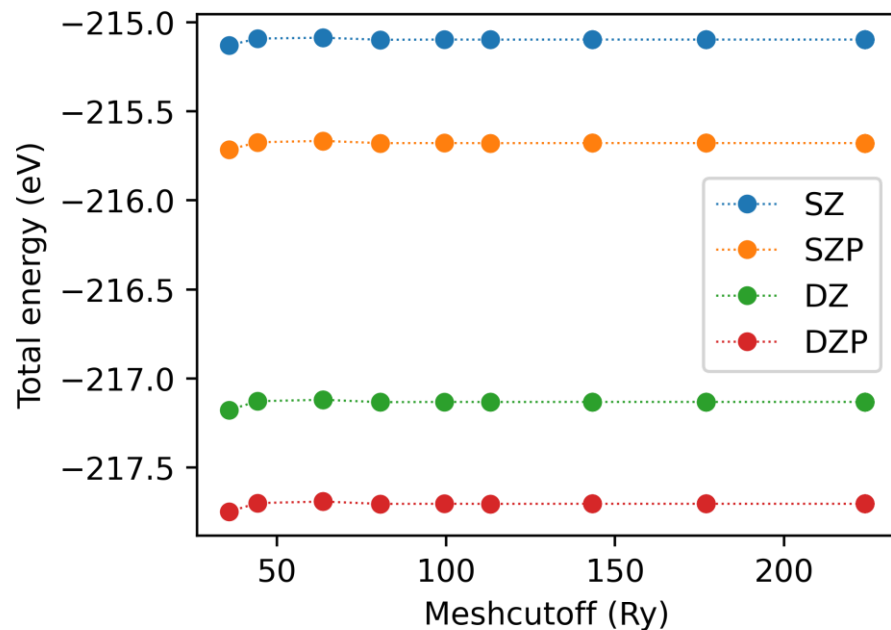


Results for methane (CH<sub>4</sub>)

# Real space grid: MeshCutoff

## Energy

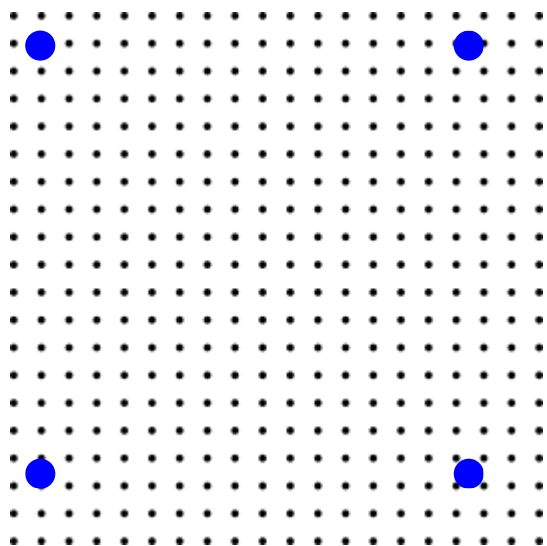
```
siesta: Final energy (eV):
```



Results for methane (CH4)



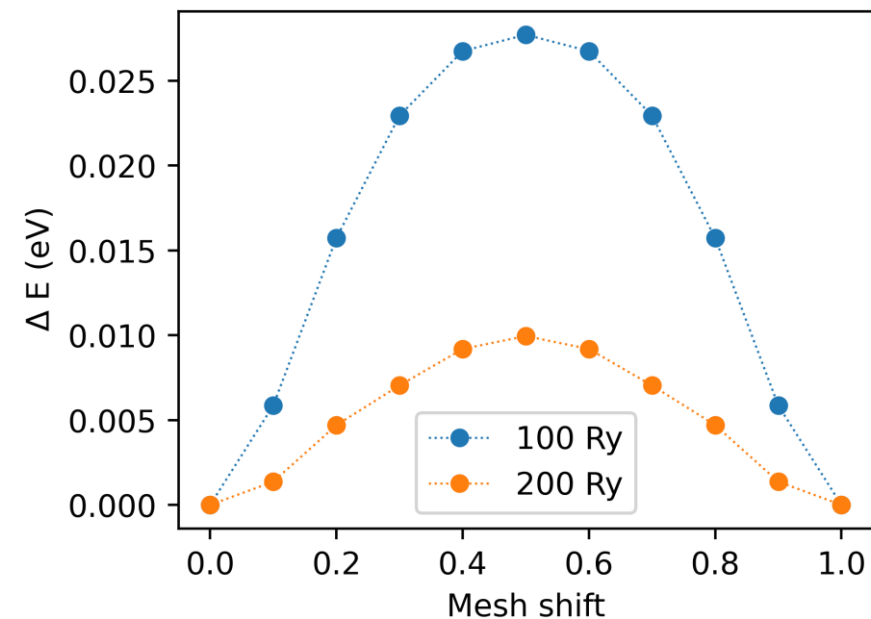
# Egg-box effect



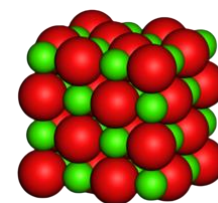
Invariant under any translation?

```
%block AtomicCoordinatesOrigin
0.0 0.0 0.0
%endblock AtomicCoordinatesOrigin
```

$$\delta z_{shift} = \left(\frac{1}{M_z}\right) \frac{1}{10}$$



Solution:  
 - Increase Meshcutoff  
 - Use "grid-cell-sampling"



Results for magnesium oxide (MgO)

# Let's try it

## Tutorials

This set of tutorials will guide you in the exploration of Siesta's features.

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**day2/03-RealSpaceGrid**

# Reciprocal space grid

Crystals

$\psi(\mathbf{r})$

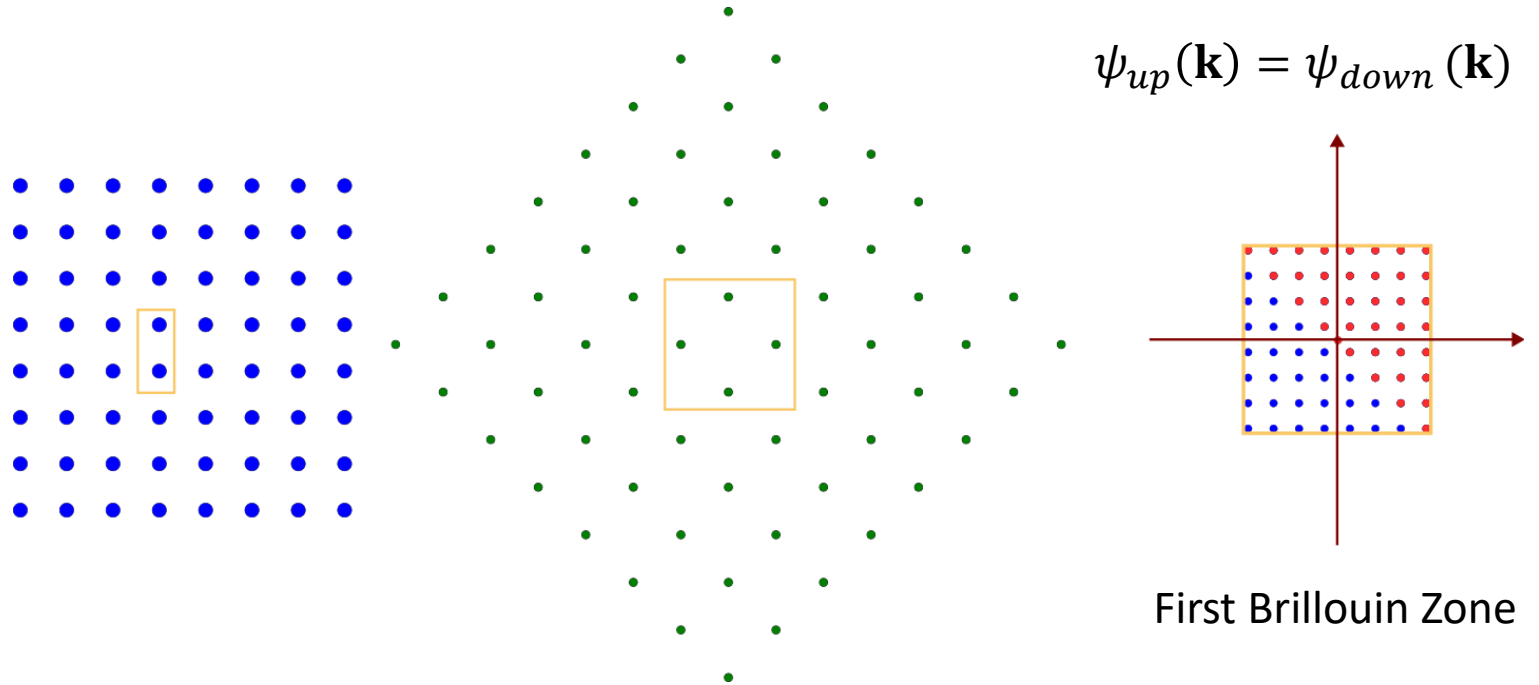
Infinite matrix

Periodicity

Reciprocal space

$$\psi_{n,\mathbf{k}+\mathbf{G}}(\mathbf{r}) = \psi_{n,\mathbf{k}}(\mathbf{r})$$

Finite matrix



# Reciprocal space grid: k-mesh

- What is it set by the user?
  - k grid cut off
  - Monkhorst Pack grid
- What is set by siesta?
  - SystemLabel.KP
- How can one decide the good value?
  - Must consider the ratio between the lattice vectors.
  - Check:
    - DOS
    - Bandstructure
  - For metallic systems more k points will be needed.

Input structure → Lattice vectors



```
kgrid_cutoff 10.0 Ang
%block kgrid Monkhorst_Pack
  6 0 0 0.0
  0 6 0 0.0
  0 0 1 0.0
%endblock kgrid_Monkhorst_Pack
```

SystemLabel.KP

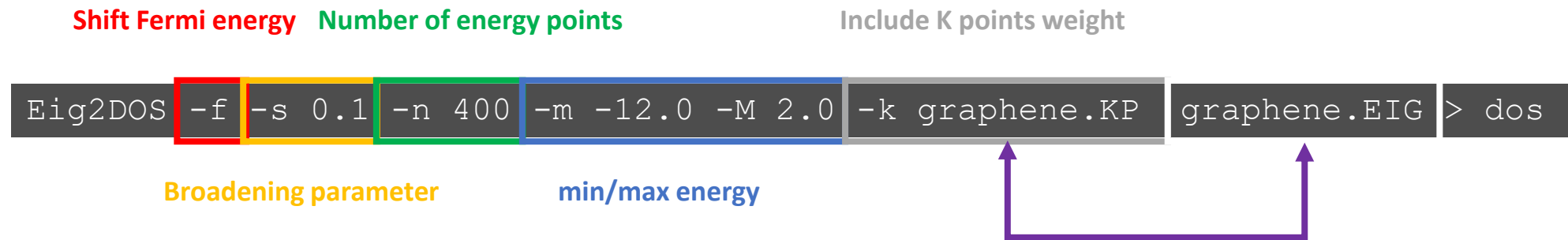
22	1	-0.447497E+00	-0.258363E+00	0.000000E+00	0.555556E-01
	2	-0.223749E+00	-0.129181E+00	0.000000E+00	0.555556E-01
	3	0.000000E+00	0.000000E+00	0.000000E+00	0.277778E-01
	4	0.671246E+00	0.387544E+00	0.000000E+00	0.277778E-01
	5	-0.447497E+00	0.111022E-15	0.000000E+00	0.555556E-01
	6	-0.223749E+00	0.129181E+00	0.000000E+00	0.555556E-01
	7	0.000000E+00	0.258363E+00	0.000000E+00	0.555556E-01
	8	0.223749E+00	0.387544E+00	0.000000E+00	0.555556E-01
	9	0.447497E+00	0.516726E+00	0.000000E+00	0.555556E-01
	10	0.671246E+00	0.645907E+00	0.000000E+00	0.555556E-01
	11	-0.447497E+00	0.258363E+00	0.000000E+00	0.555556E-01
	12	-0.223749E+00	0.387544E+00	0.000000E+00	0.555556E-01
	13	0.000000E+00	0.516726E+00	0.000000E+00	0.555556E-01
	14	0.223749E+00	0.645907E+00	0.000000E+00	0.555556E-01
	15	0.447497E+00	0.775088E+00	0.000000E+00	0.555556E-01
	16	0.671246E+00	0.904270E+00	0.000000E+00	0.555556E-01
	17	-0.447497E+00	0.516726E+00	0.000000E+00	0.277778E-01
	18	-0.223749E+00	0.645907E+00	0.000000E+00	0.277778E-01
	19	0.000000E+00	0.775088E+00	0.000000E+00	0.277778E-01
	20	0.223749E+00	0.904270E+00	0.000000E+00	0.277778E-01
	21	0.447497E+00	0.103345E+01	0.000000E+00	0.277778E-01
	22	0.671246E+00	0.116263E+01	0.000000E+00	0.277778E-01

# DOS: Eig2DOS

Shift Fermi energy    Number of energy points    Include K points weight

```
Eig2DOS -f -s 0.1 -n 400 -m -12.0 -M 2.0 -k graphene.KP graphene.EIG > dos
```

Broadening parameter    min/max energy

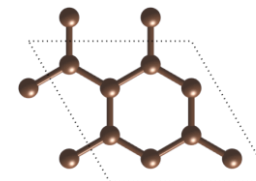
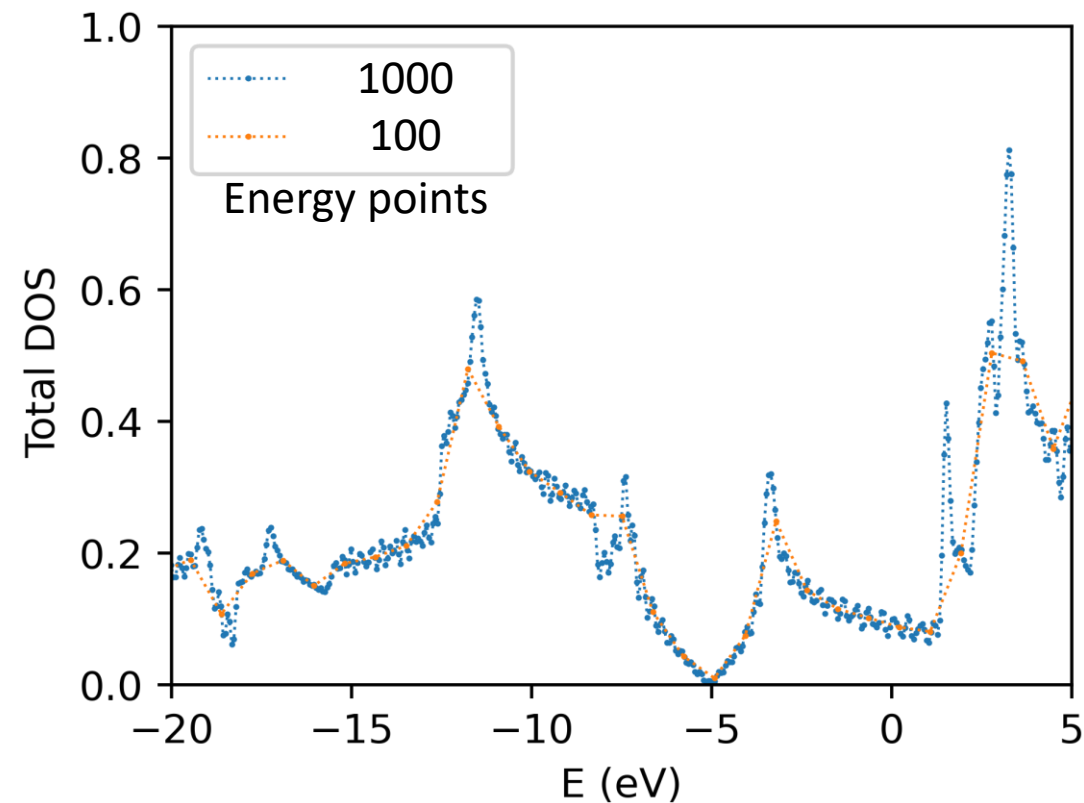


# Eig2DOS output

```

EIG2DOS: Utility for SIESTA to obtain the electronic density of states
# E. Artacho, Apr 1999, A. Garcia, Apr 2012
# Nick R. Papior, Feb 2017
# -----
# Eigenvalues calculated from a spin-polarized calculation
# Eigenvalues read from graphene.EIG
# Kpoint weights read from graphene.KP
# Using smearing parameter: 0.1000
# Using 400 points in the energy range
# Selected bands: 1 to: 26
# Emin, Emax in file for selected band(s): -24.2236335 143.6658020
# Nbands, Nspin, Nk = 26 2 5
# E_F = -5.0301 eV --> (shifted to ZERO)
# Broadening = 0.1000 eV
#
# E N(up) N(down) Ntot
-12.000000 0.000000 0.000000 0.000000
-11.964912 0.000000 0.000000 0.000000
-11.929825 0.000000 0.000000 0.000000
-11.894737 0.000000 0.000000 0.000000
-11.859649 0.000000 0.000000 0.000000
-11.824561 0.000000 0.000000 0.000000
-11.789474 0.000000 0.000000 0.000000
-11.754386 0.000000 0.000000 0.000000
-11.719298 0.000000 0.000000 0.000000
-11.684211 0.000000 0.000000 0.000000
-11.649123 0.000000 0.000000 0.000000
-11.614035 0.000000 0.000000 0.000000
-11.578947 0.000000 0.000000 0.000000
-11.543860 0.000000 0.000000 0.000000
-11.508772 0.000000 0.000000 0.000000
-11.473684 0.000000 0.000000 0.000000
-11.438596 0.000000 0.000000 0.000000
-11.403509 0.000000 0.000000 0.000000
-11.368421 0.000000 0.000000 0.000000
-11.333333 0.000000 0.000000 0.000000
-11.298246 0.000000 0.000000 0.000000
-11.263158 0.000000 0.000000 0.000000
-11.228070 0.000000 0.000000 0.000000
-11.192982 0.000000 0.000000 0.000000
-11.157895 0.000000 0.000000 0.000000
-11.122807 0.000000 0.000000 0.000000
-11.087719 0.000000 0.000000 0.000000
-11.052632 0.000000 0.000000 0.000000
-11.017544 0.000000 0.000000 0.000000
-10.982456 0.000000 0.000000 0.000000
-10.947368 0.000000 0.000000 0.000000
-10.912281 0.000000 0.000000 0.000001

```



Results for graphene

# Bandstructure: gnubands

```
%block Bandlines
1 0.5000000000 0.0000000000 0.0000 M
30 0.0000000000 0.0000000000 0.0000 \Gamma
45 0.3333333333 0.3333333333 0.0000 K
30 0.5000000000 0.5000000000 0.0000 M
%endblock BandLines
```

SystemLabel.bands

- G : print GNUplot commands for correct labels to stderr  
Suggested usage: prog options 2> bands.gplot 1> bands.dat  
gnubands [options] 1> bands.dat 2> bands.gplot  
and then:  
gnuplot -persist bands.gplot
- s arg : only plot selected spin bands [1,ns핀]
- F : shift energy to Fermi-level
- b arg : first band to write
- B arg : last band to write
- e arg : minimum energy to write  
: If -F set, will be with respect  
: to Fermi level
- E arg : maximum energy to write  
: Note, see -e
- o file : specify output file (instead of piping)  
: if used with -G a file name file.gplot will be created

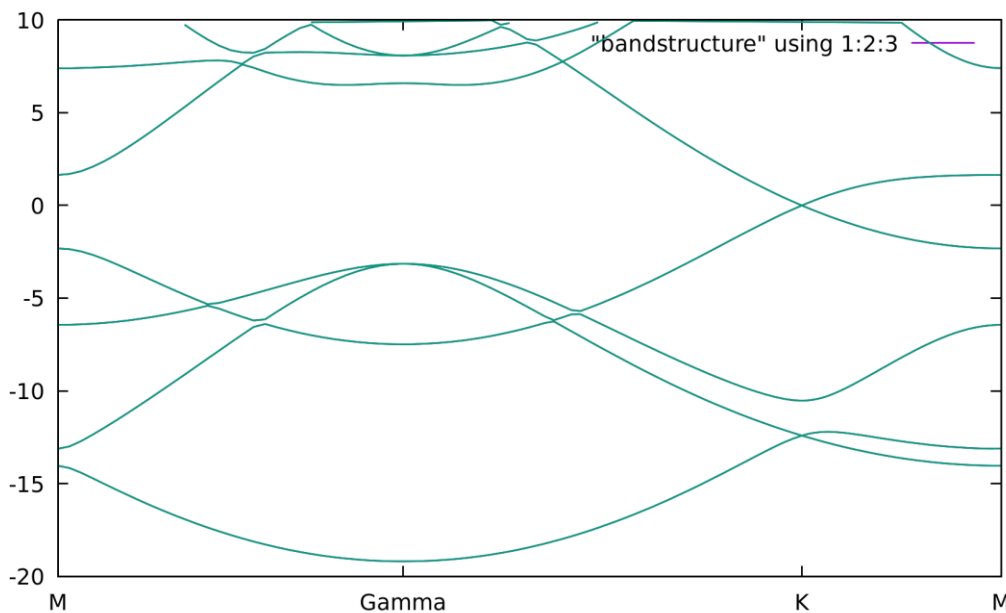
```
gnubands -F -G -o bandstructure -E 10 -e -20 SystemLabel.bands
```

Shift Fermi energy      Shift Fermi energy      Min/max energy

# Bandstructure

```
gnubands -F -G -o bandstructure -E 10 -e -20 *.bands
gnuplot -persist bandstructure.gplot
```

```
set xtics ("M" 0.000000, "Gamma" 0.775088, "K" 1.670083, "M" 2.117581)
plot "bandstructure" using 1:2:3 with lines lc variable
# -- Use line below for single-color#plot "bandstructure" with lines
```



Results for graphene

```
# GNUBANDS: Utility for SIESTA to transform bands output into
#Gnuplot format
#
# Emilio Artacho, Feb. 1999 # Alberto Garcia, May 2012
# Nick Papior, April 2013, July 2016
# -----
# Bands for all spins
# E_F / orig = 0.0000 -5.0301
# k_min, k_max = 0.0000 2.1176
# E_min, E_max = -20.0000 10.0000
# Nbands, Nspin, Nk = 26 2 106
# Using min_band, max_band = 1 26
# Total number of bands = 26
#
# k E[eV]
# -----
0.000000 -14.038730 1
0.025836 -14.158130 1
0.051673 -14.413430 1
0.077509 -14.707530 1
0.103345 -15.009230 1
0.129181 -15.308430 1
0.155018 -15.601030 1
0.180854 -15.885030 1
0.206690 -16.159330 1
0.232526 -16.423330 1
0.258363 -16.676430 1
0.284199 -16.918530 1
0.310035 -17.149230 1
```



# Let's try it

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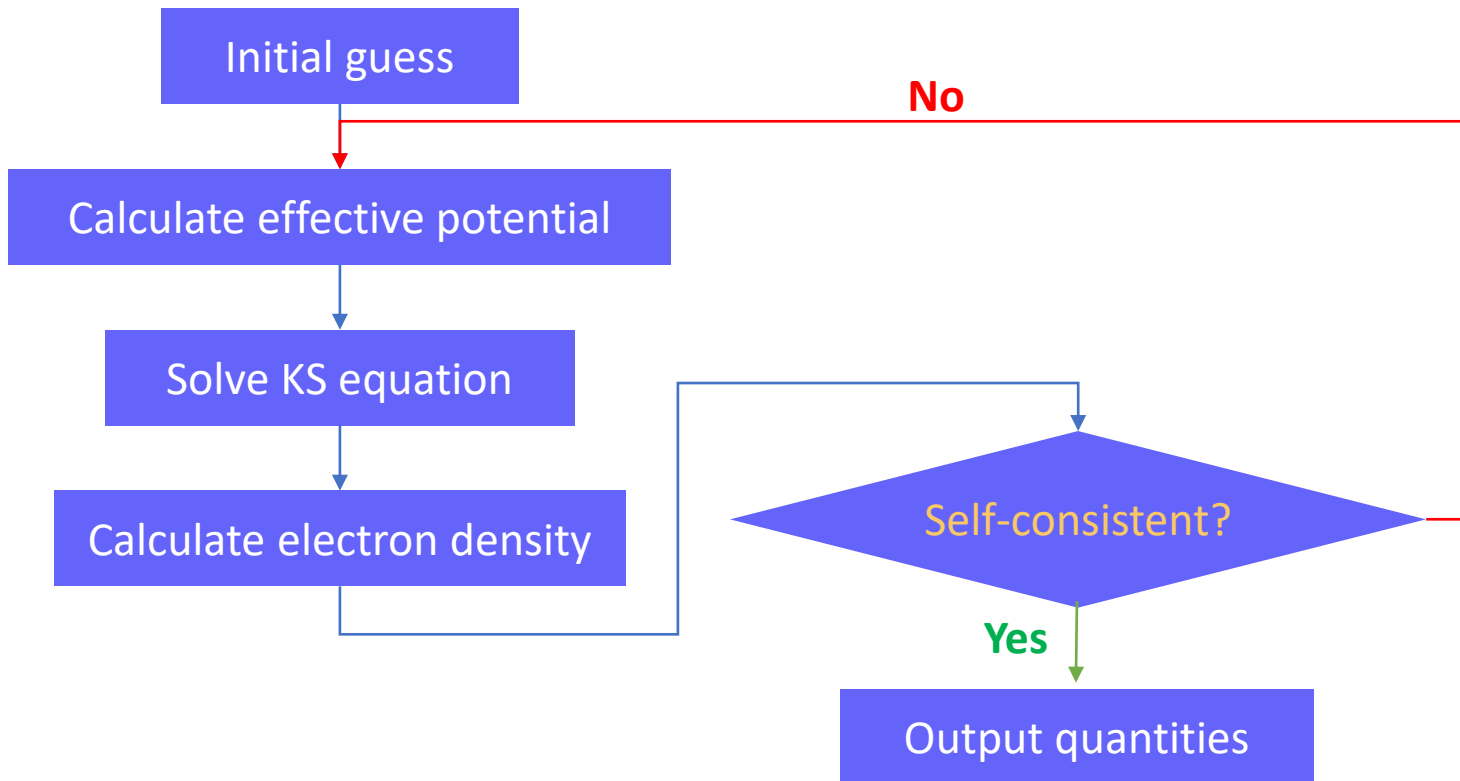
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### day2/04-KpointSampling

SCF convergence

# SCF convergence



- The physical quantity that is mixed:
  - Density matrix
  - Hamiltonian matrix
- Mixing algorithm:
  - Linear
  - Broyden
  - Pulay } N previous steps

# SCF convergence

- SCF.Mix [default Hamiltonian]:
  - Density -> for systems hard to converge
  - Hamiltonian
- SCF.MixerMethod [default Pulay]
  - Linear
  - Pulay
  - Broyden
- SCF.Mixer.Weight [default 0.3]
  - 0.001 systems hard to converge ->a lot of steps
  - 0.4 systems easy to converge -> reduce steps
- SCF.Mixer.History [default 2]
- Max.SCF.Iterations [default 1000]
- SCF.DM.Converge F [default T]
- SCF.H.Converge F [default T]

All of them strongly dependent on the system!!

```
SCF.Mix Hamiltonian
SCF.MixerMethod Pulay
SCF.Mixer.Weight 0.3
```

```
SCF.DM.Tolerance 10-4
SCF.H.Tolerance 10-3 eV
```

```
Max.SCF.Iterations 75
SCF.MixerMethod pulay
SCF.Mixer.Weight 0.2
```

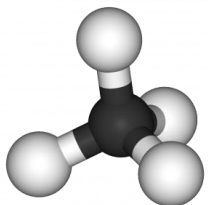
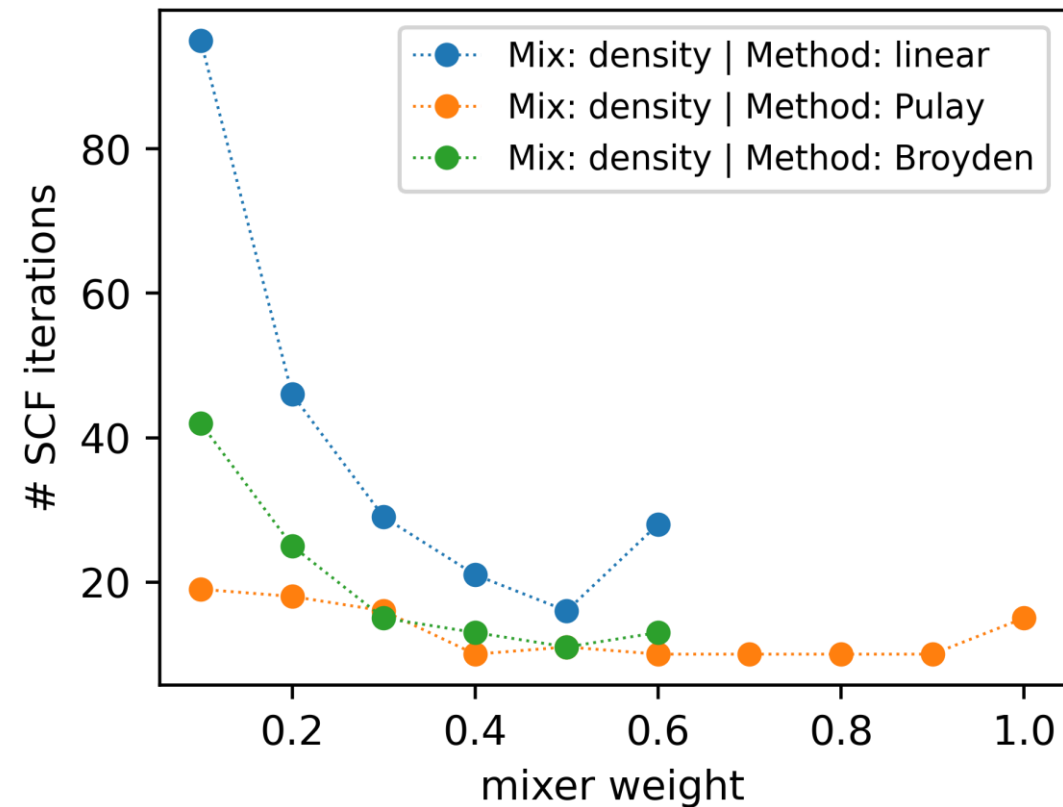
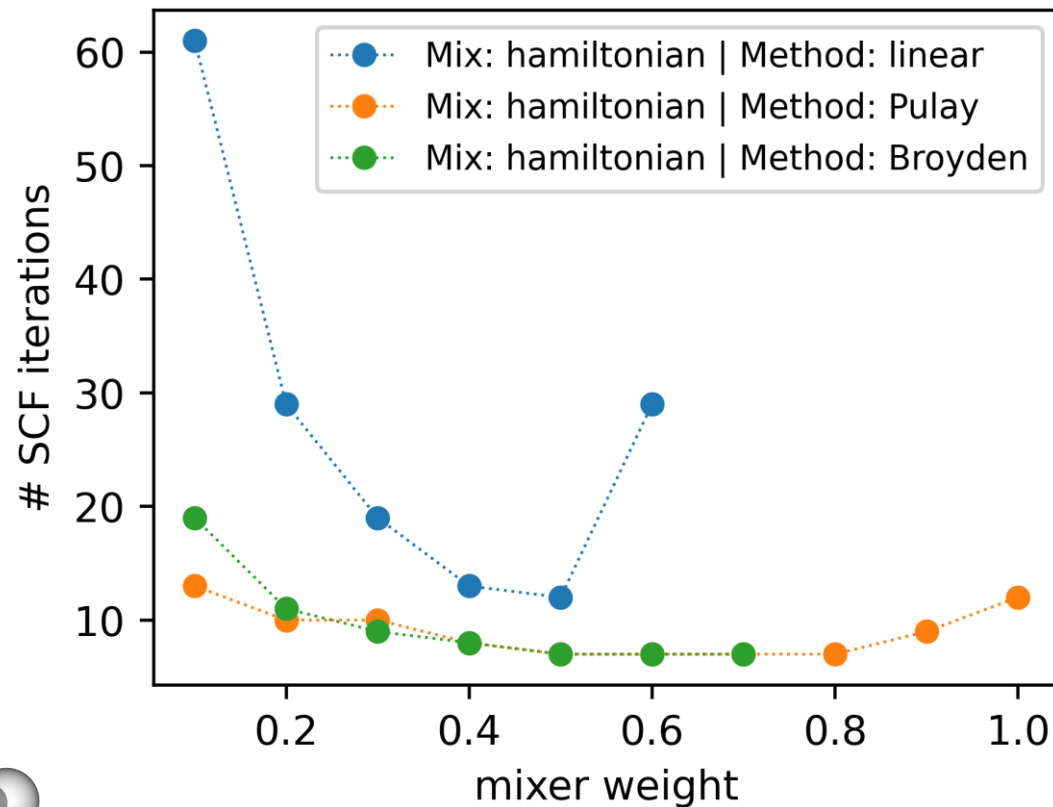
```
SCF.Mixer.History 5
```

More advanced options ... (manual)

# SCF convergence

SCF cycle converged

SCF\_NOT\_CONV:



Results for methane (CH4)

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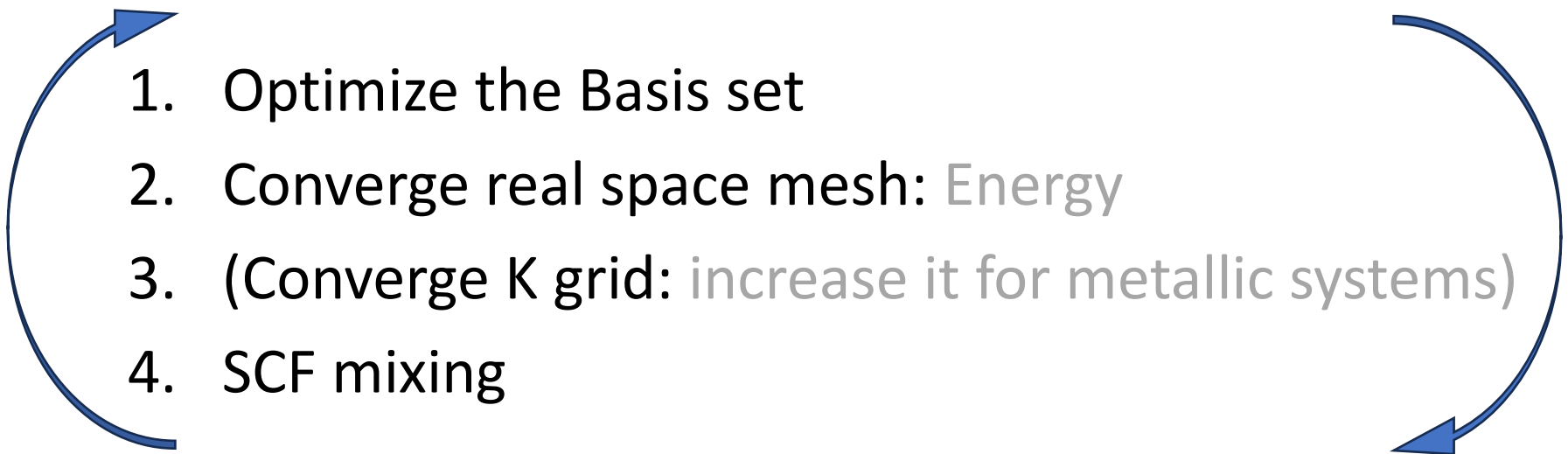
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**day2/05-SCF-Options**

# How do I converge the whole calculation?

- 
1. Optimize the Basis set
  2. Converge real space mesh: Energy
  3. (Converge K grid: increase it for metallic systems)
  4. SCF mixing



Thank you for your attention

